



Design & Verification of Restart-robust Industrial Control Software

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Outline

Introduction

- Model Checking Industrial Control Software
- Motivation

Modelling the Restart Semantics

- Verification of Restart-robustness
- Synthesis of Safe Retain Configurations

Counterexample-Guided Parameter Synthesis

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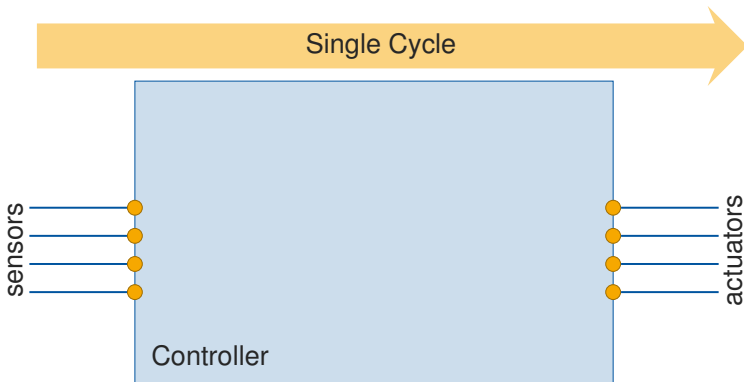
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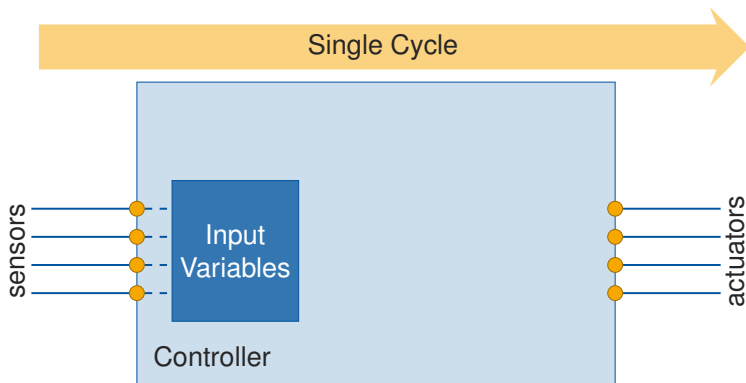
Mode of Operation

- ▶ Industrial controllers operate in **program execution cycles**
- ▶ Realise **reactive systems**



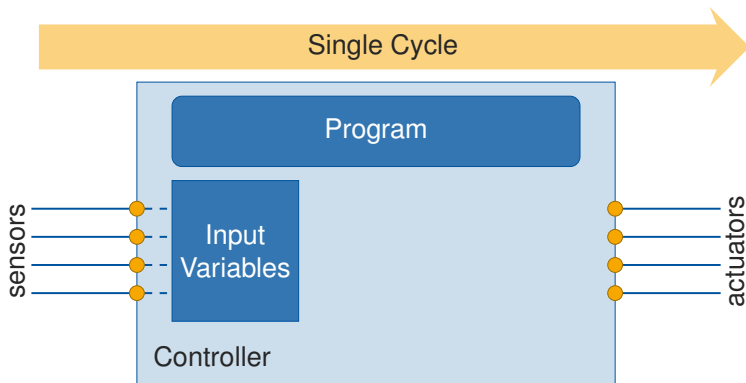
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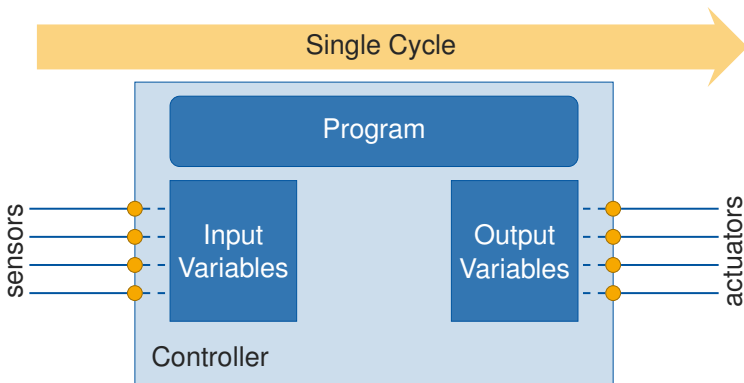
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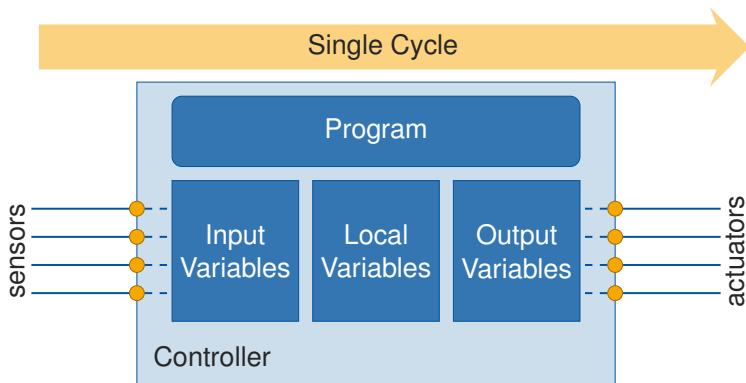
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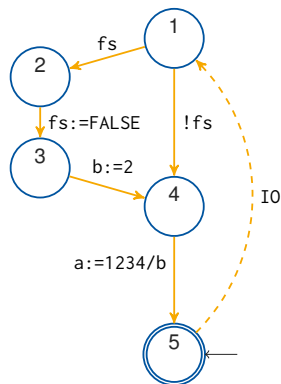
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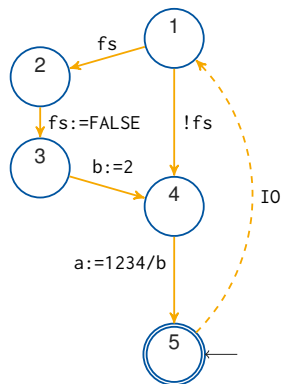
Software & Specifications

- ▶ Program as **Control Flow Automaton**
- ▶ Intermediate states are not observable
- ⇒ Automation engineers and specs always refer to the observable state
- ▶ Most specifications can be formalised via invariants or temporal logics
- ▶ Off-the-shelf verifier backend checks formalised program w.r.t. the specification



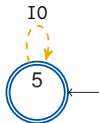
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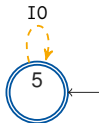
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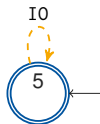
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Symbolic Model Verifier (SMV)

- ▶ Uses symbolic transition system
- ▶ Transition relation

$$T \subseteq \underbrace{Loc \times \vec{V}}_{\text{pre}} \times \underbrace{Loc \times \vec{V}}_{\text{post}}$$

Constrained Horn Clauses (CHC)

- ▶ Uses formulas of the form

$$\forall \vec{V} \underbrace{p_1(\vec{V}) \wedge \dots \wedge p_k(\vec{V}) \wedge \varphi}_{\text{body}} \rightarrow h(\vec{V})$$

- ▶ Predicates p_i typically characterise values at locations

Example: Invariant $a \geq 0$ at cycle end

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Retain Variables

- ▶ Applications are often **safety critical**
- ▶ **Power outage** or manual restart **should not affect correctness**
- ⇒ Controllers feature **battery-backed memory** to retain variables

Example

Retain drill's position in automated processing of workpieces

- ▶ Assignments to such variables have **unspecified semantics**
- ▶ Prominent semantics:
 - Immediate writing to the battery-backed memory
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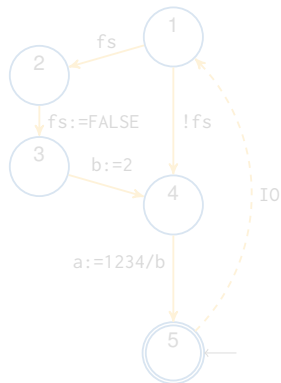
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Restart-robustness

Program is **restart-robust w.r.t. a spec**, if it complies with the spec in the context of restarts

Restart-robustness w.r.t. invariant $a \geq 0$

- ▶ Initialised with $[fs \mapsto true, a \mapsto 0, b \mapsto 0]$
- ▶ The flag fs is retained
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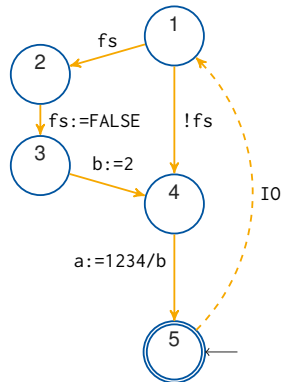


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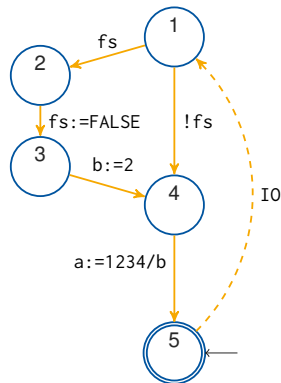


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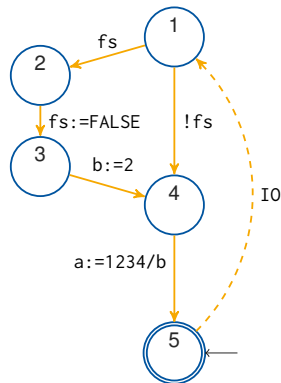


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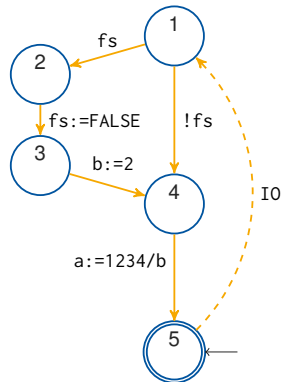


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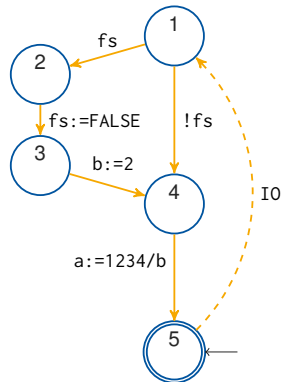


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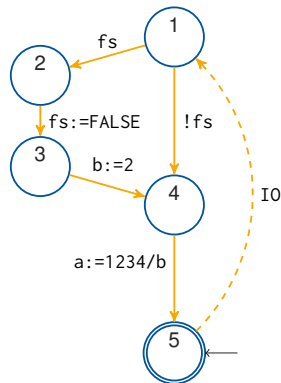


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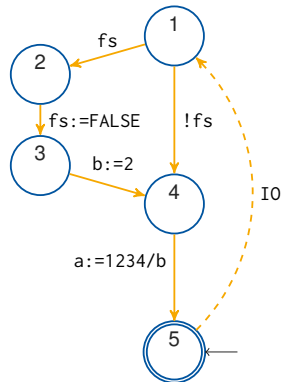


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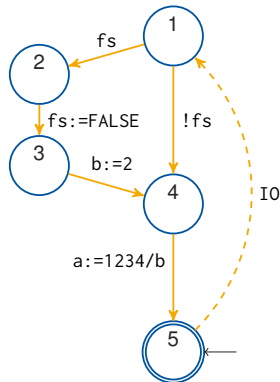


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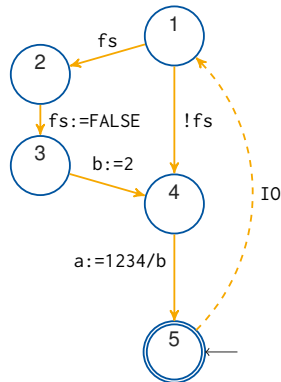


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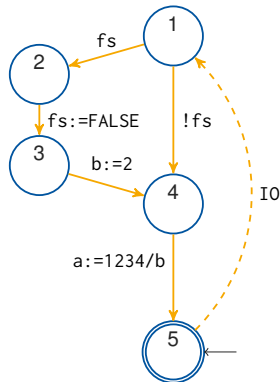


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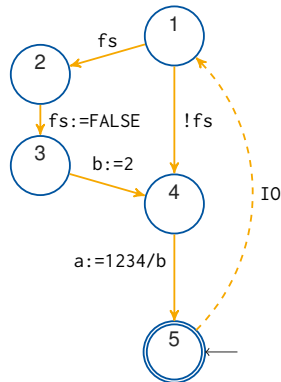


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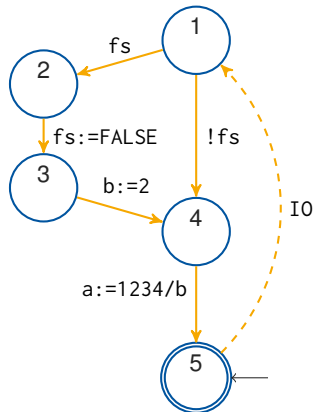
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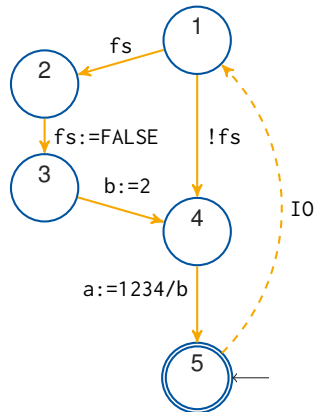
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 - ▶ Observation: In case of restart, operations since last cycle are irrelevant
- ⇒ Model as nondeterministic choice: restart in next cycle?



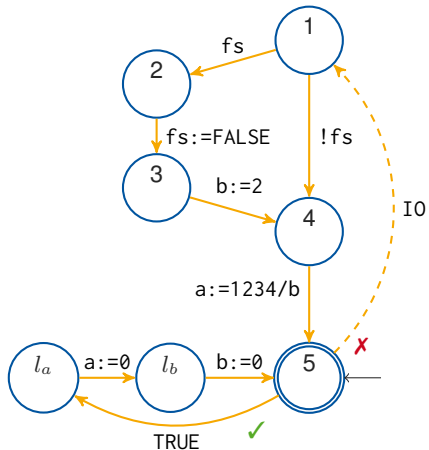
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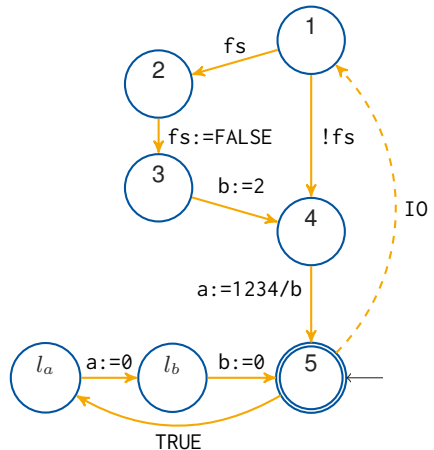
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Immediate Write Semantics

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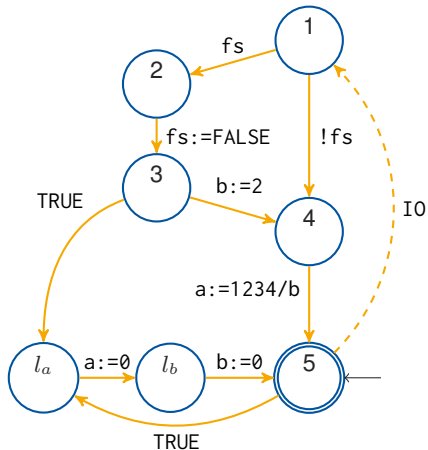
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- ▶ Instrumentation **enables checking restart-robustness** w.r.t. a spec via common verifier backends
 - ▶ **Doesn't help with finding** safe configuration of retain variables
- ⇒ Parametrise the CFA with the configuration of retain variables

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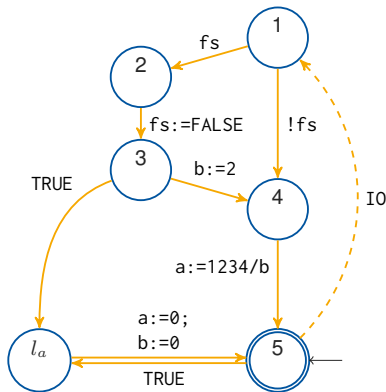
CHC-based Parameter Synthesis

- ▶ Add **Boolean parameter** `ret_v` for each non-retain variable `v`
- ▶ Add **guarded options** to restart
- ▶ Derived CHCs check **whether all configurations** are robust

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- ▶ Parameter synthesis is

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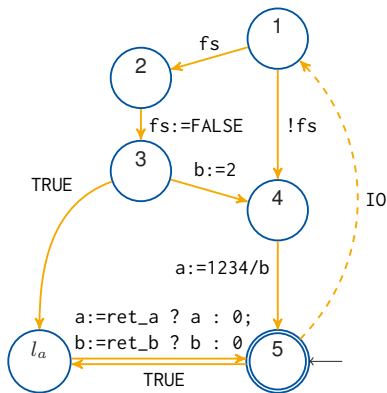
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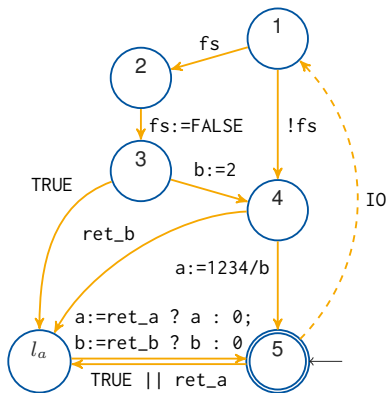
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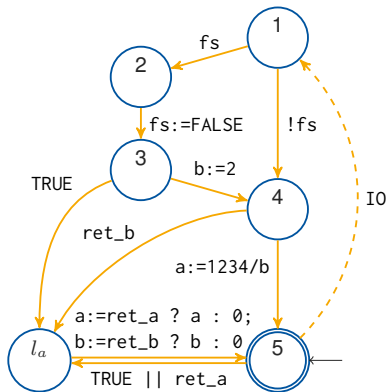
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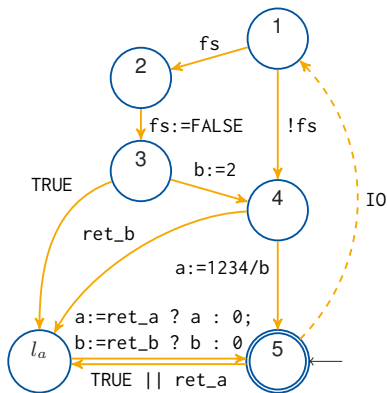
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- ▶ Add **Boolean parameter** `ret_v` for each non-retain variable `v`
- ▶ Add **guarded options** to restart
- ▶ Derived CHCs check **whether all configurations** are robust

$$\forall \vec{V} \underbrace{\dots}_{\text{body}} \rightarrow h(\vec{V})$$

- ▶ Parameter synthesis is

$$\exists \vec{V}_{par} \forall \vec{V} \setminus \vec{V}_{par} \dots \rightarrow h(\vec{V})$$

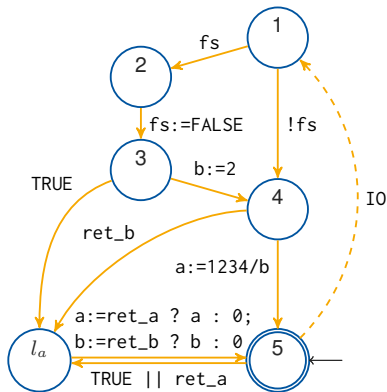


SMV-based Parameter Synthesis

- ▶ **No quantifiers** for variables
- ⇒ Integrate parameter choice prepended to entry
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Invariant $a \geq 0$

Quantification via CTL:

$$EX\ AG(pc = 5 \rightarrow a \geq 0)$$


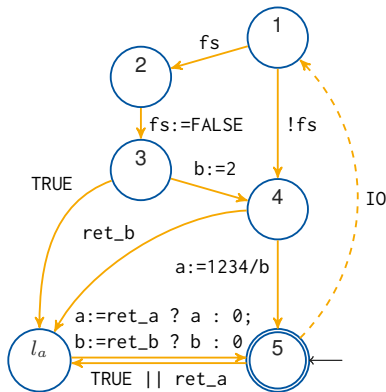
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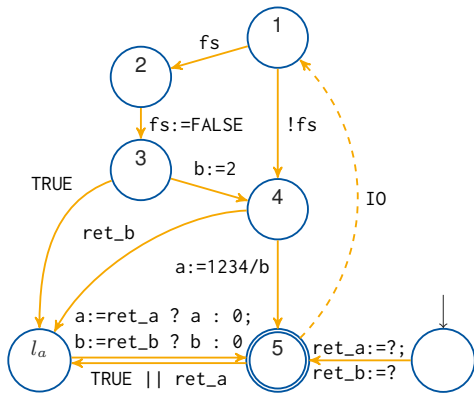
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Experiments on implementation of **PLCopen Safety** library:

- ▶ **Elementary modules** implementing particular safety concepts
- ▶ User examples **composed** of those

Specifications:

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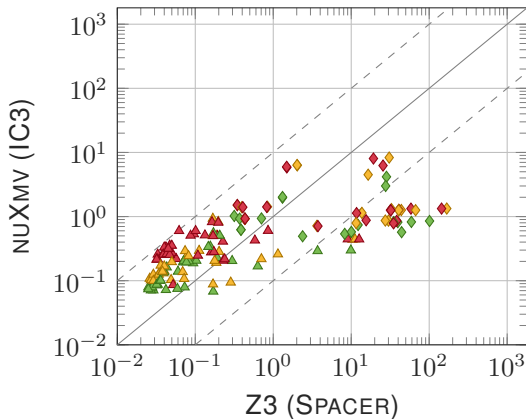
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Restart-robustness Checking



Elementary Modules

- ▲ No Restarts
- ▲ Delayed Write
- ▲ Immediate Write

Composite Modules

- ◆ No Restarts
- ◆ Delayed Write
- ◆ Immediate Write

Figure: Time [s] spent checking restart-robustness w.r.t. each spec

Parameter Synthesis

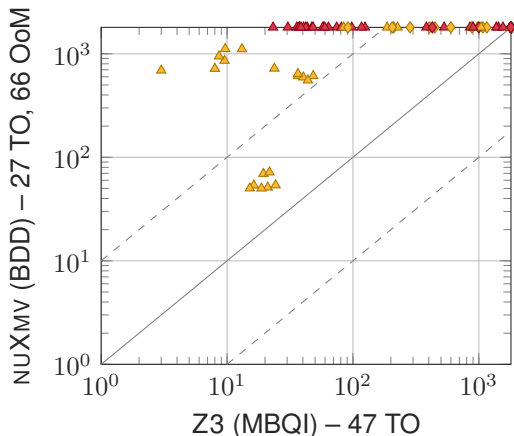


Figure: Time [s] spent on synthesis of restart-robust configurations

Can we do better?

Observations:

- ▶ $\exists\forall$ -quantified Horn clauses **harder** than regular CHCs
- ▶ Our **special case**: existential quantification over Booleans

Idea:

- ▶ Manage choice of parameters and **reuse efficient procedures** for reasoning about restart-robustness for **fixed parameters**
- ▶ **Over-approximate** set of “safe” parameters and **refine it** while counterexamples exist

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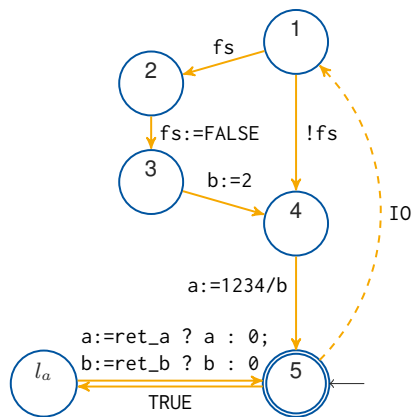
- ▶ Make the program restart-robust w.r.t. $a \geq 0$ under **delayed writes**
- ▶ Let fs be required to be **retained**

Process:

1. Start with $safe(\vec{V}_{par}) = true$
2. Backend finds counterexample

$$c = \neg ret_a \wedge \neg ret_b$$
3. Find subset of violating params

$$c_g = \neg ret_b$$
4. Refine $safe(\vec{V}_{par}) = true \wedge \neg c_g$
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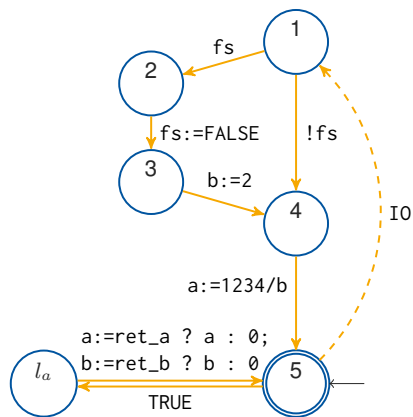
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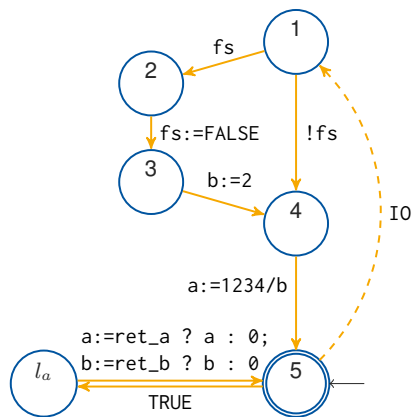
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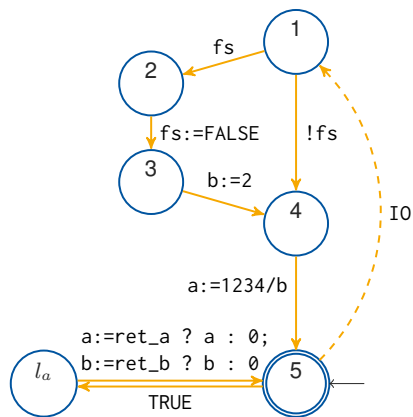
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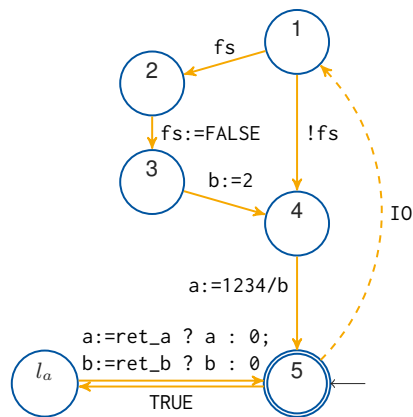
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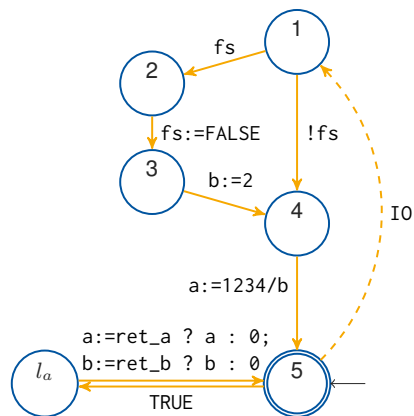
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Improved Results

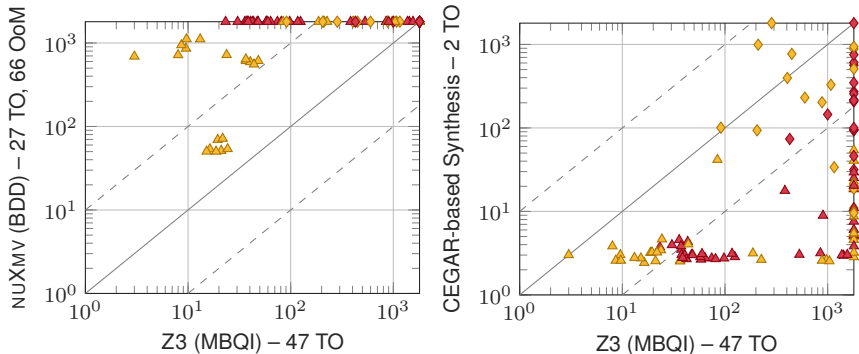


Figure: Time [s] spent on synthesis of restart-robust configurations

Summary

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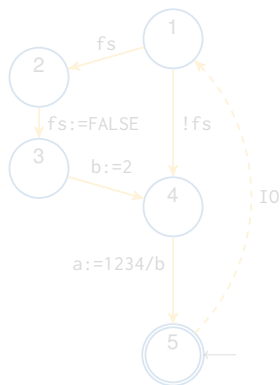
Related Work

- ▶ [Hau+15] assumes **delayed write** semantics and adapts **static value analysis** to distinguish between variables' values before and after a restart
- ▶ **Crash recoverability** of C programs [KY16] is a related problem, using a similar modelling, but **differing** from restart-robustness in terms of **requirements and program transformations**
- ▶ **SMV-based parameter synthesis** for models of gene regulatory networks [Bat+10]
- ▶ Our **counterexample-guided approach** is most similar to [Cim+13] but does not require quantifier elimination, is independent of the chosen theory to model values, and works with any CHC-solving algorithm

PLC Software

- ▶ Written in textual & graphical languages from IEC 61131-3
- ▶ Features **no recursion**
- ⇒ Formalised as **Control Flow Automaton (CFA)**

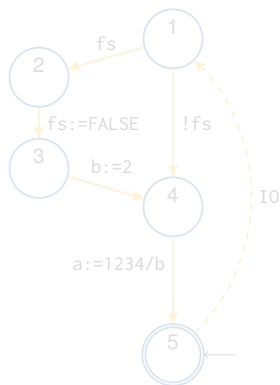
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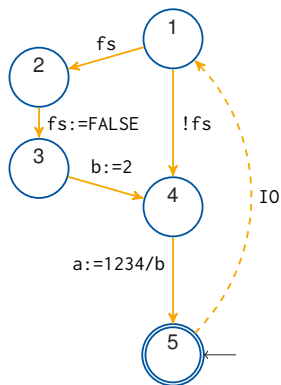
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Algorithm 1: SynthRetainConf(P, φ)

Input : Program $P = (\vec{X} \uplus \vec{X}_{\text{par}}, \vec{X}_{\text{in}}, \mathcal{A}, l_{\text{EoC}}, l_{\text{EoC}}, \text{def})$ with parametrised retains
Predicate $\varphi(\vec{X})$ characterising safe states

Variables: Predicate $\text{safe}(\vec{X}_{\text{par}})$ charactering parameters that do not lead to violations
Universally quantified Horn clauses \mathcal{H}

```

1   $\mathcal{H} \leftarrow \text{toHorn}(P)$  // Represent program as  $\forall$ CHCs
2   $(\vec{V}, I, T) \leftarrow \text{toSymbTS}(P)$  // and as symbolic transition system
3   $\text{safe}(\vec{X}_{\text{par}}) \leftarrow \text{true}$  // All parameters are assumed to be safe
4  while  $\neg \text{sat}(\mathcal{H} \cup \{\varphi(\vec{X}) \leftarrow p_{\text{EoC}}(\vec{X} \uplus \vec{X}_{\text{par}}), \text{safe}(\vec{X}_{\text{par}})\})$  do //  $\exists$  violating run?
5  |    $k \leftarrow \text{length of violating run}$ 
6  |    $c_{\text{par}} \leftarrow \text{cube of chosen (Boolean) parameter values in violating run}$ 
7  |   foreach  $\text{lit in } c_{\text{par}}$  do
8  |   |    $\bar{c}_{\text{par}} \leftarrow c_{\text{par}}$  with negated lit // Flip literal
9  |   |   if  $\text{sat}(I(\vec{V}) \wedge \bigwedge_{0 \leq i < k} T(\vec{V}_i, \vec{V}_{i+1}) \wedge \bar{c}_{\text{par}} \wedge \neg \varphi(\vec{X}_k))$  then // Still violating?
10 |   |   |    $c_{\text{par}} \leftarrow c_{\text{par}} \setminus \text{lit}$  // Drop literal
11 |   |    $\text{safe}(\vec{X}_{\text{par}}) \leftarrow \text{safe}(\vec{X}_{\text{par}}) \wedge \neg c_{\text{par}}$  // Block unsafe parameters
12 return  $\text{safe}(\vec{X}_{\text{par}})$  // (Potentially empty) region of safe parameters

```

References I

- [Bat+10] Grégory Batt et al. “Efficient parameter search for qualitative models of regulatory networks using symbolic model checking”. In: *Bioinformatics* 26.18 (2010).
- [Cim+13] Alessandro Cimatti et al. “Parameter synthesis with IC3”. In: *Formal Methods in Computer-Aided Design, FMCAD 2013, Portland, OR, USA, October 20-23, 2013*. 2013, pp. 165–168.

References II

- [Hau+15] Stefan Hauck-Stattelmann et al. “Analyzing the Restart Behavior of Industrial Control Applications”. In: *FM 2015: Formal Methods - 20th International Symposium, Oslo, Norway, June 24-26, 2015, Proceedings*. 2015, pp. 585–588.
- [KY16] Eric Koskinen and Junfeng Yang. “Reducing crash recoverability to reachability”. In: *Proceedings of the 43rd Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages, POPL 2016, St. Petersburg, FL, USA, January 20 - 22, 2016*. 2016, pp. 97–108.